

6.1 Warm-Up

What is a ratio?

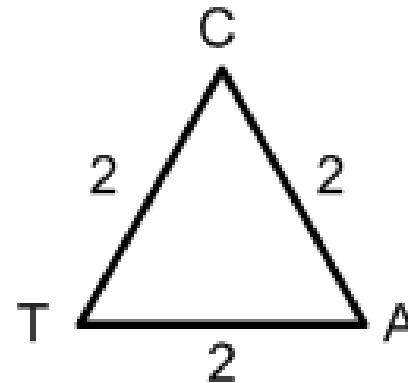
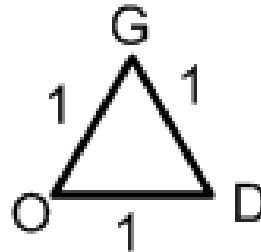
Compares 2 #'s

What are the different ways to write a ratio?

$\frac{a}{b}$ $a:b$ a to b

What's the ratio of the side lengths in $\triangle CAT$ to the sides lengths in $\triangle DOG$?

2:1



Example of equivalent ratios:

Ratios are usually written in simplest form!!

What is the ratio of the width to the length?



$$\frac{7}{21} = \frac{1}{3}$$

Simplify the ratios:

1. 24 yards to 3 yards 8 to 1

2. 64 m : 6 m 32 : 3

3. 150 cm : 6 m 25 cm : 1 m

25 cm : 100 cm

1 : 4

4. $\frac{5 \text{ ft}}{20 \text{ in}} = \frac{1 \text{ ft}}{4 \text{ in}}$
 $= \frac{12 \text{ in}}{4 \text{ in}} = \frac{3}{1}$

We know that the area of a rectangular garden is 108 square feet, and that the ratio of the length to width is 4:3. Find the length and width of fence needed to enclose the garden.

$$A = 108 \text{ ft}^2$$

$$\textcircled{1} A = l \cdot w$$

$$l:w \rightarrow 4:3$$

$$108 = 4x \cdot 3x \quad \textcircled{3}$$

$$\textcircled{2} l = 4x = 4 \cdot 3 = 12'$$

$$w = 3x = 3 \cdot 3 = 9'$$

$$\frac{108}{12} = \frac{12x^2}{12}$$

$$\sqrt{9} = \sqrt{x^2}$$

$$3 = x$$

$$\textcircled{5}$$

$$\textcircled{4}$$

The measures of the angles of $\triangle CMT$ are in the extended ratio 2:3:4. Find the measures of the angles.

$$m\angle C + m\angle M + m\angle T = 180$$

$$2x + 3x + 4x = 180$$

$$9x = 180$$

$$x = 20$$

$$\begin{array}{l} 2 \cdot 20 = 40^\circ \\ 3 \cdot 20 = 60^\circ \\ 4 \cdot 20 = 80^\circ \end{array}$$

What is a proportion?

$$\frac{a}{b} = \frac{c}{d}$$

What is the Cross Products Property?

$$bc = ad$$

Solve the proportions:

a. $\frac{\cancel{5}}{\cancel{10}} = \frac{x}{16}$

$$\frac{1}{2} = \frac{x}{16}$$

$$2x = 16$$

$$x = 8$$

b. $\frac{1}{y+1} = \frac{2}{3y}$

$$3y = 2(y+1)$$
$$3y = 2y + 2$$
$$y = 2$$

As part of a science project, you need to estimate the number of blue spruce trees in a 50 acre forest. You count 36 trees in 3 acres and the trees seem to be evenly distributed. Estimate the total number of blue spruce trees in the forest.

$$12 \frac{\cancel{36} \text{ trees}}{\cancel{3} \text{ acres}} = \frac{X \text{ trees}}{50 \text{ acres}}$$

$$X = 12 \cdot 50 = \boxed{600 \text{ trees}}$$

Geometric mean:

$$\frac{a}{x} = \frac{x}{b}$$

$$x^2 = ab$$

$$\sqrt{x^2} = \sqrt{ab}$$

$$x = \sqrt{ab}$$

Find the geometric mean of 36 and 54.

$$\begin{aligned} x &= \sqrt{36 \cdot 54} \\ &= \sqrt{36} \sqrt{54} \\ &= 6 \sqrt{9 \cdot 6} \end{aligned} \rightarrow \begin{aligned} &= 6 \sqrt{9} \sqrt{6} \\ &= 6 \cdot 3 \sqrt{6} \\ &= \boxed{18 \sqrt{6}} \end{aligned}$$

Find the geometric mean.

1. 12 and 27

$$\begin{aligned} X &= \sqrt{12 \cdot 27} \\ &= \sqrt{4 \cdot 3 \cdot 9 \cdot 3} \\ &= \sqrt{4} \sqrt{9} \sqrt{3 \cdot 3} \\ &= 2 \cdot 3 \sqrt{9} \\ &= 6 \cdot 3 = \boxed{18} \end{aligned}$$

2. 18 and 54

$$\begin{aligned} X &= \sqrt{18 \cdot 54} \\ &= \sqrt{9 \cdot 2 \cdot 9 \cdot 6} \\ &= \sqrt{9} \sqrt{9} \sqrt{2 \cdot 6} \\ &= 3 \cdot 3 \sqrt{12} \\ &= 9 \sqrt{12} \\ &= 9 \sqrt{4 \cdot 3} = 9 \cdot 2 \sqrt{3} = \boxed{18\sqrt{3}} \end{aligned}$$

3. 16 and 18

$$\begin{aligned} X &= \sqrt{16 \cdot 18} \\ &= \sqrt{16} \sqrt{9 \cdot 2} \\ &= 4 \sqrt{9} \sqrt{2} \\ &= 4 \cdot 3 \sqrt{2} \\ &= \boxed{12\sqrt{2}} \end{aligned}$$

what jobs use the geometric mean

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Homework:

pp 360-363

#'s 4-36E, 42, 46,
58, 59, 61, 65

OR

#'s 8, 18, 22, 36, 42, 46, 58